

### Number Machines

$$5 \xrightarrow{+ 3} 8 \xrightarrow{\times 10} 80$$

$$5 \xrightarrow{\times 2} 10 \xrightarrow{- 4} 6$$

$$4 \xrightarrow{\times 6} 24 \xrightarrow{+ 5} 29$$

$$5 \xrightarrow{\times 5} 25 \xrightarrow{- 5} 20$$

Match the flow diagram to the expression:

5 x a + 4  $5a+4$

5 + a x 4  $4(5+a)$

5 x a - 4  $5a-4$

4 x a + 5  $4a+5$

a x 4 - 5  $4a - 5$

Draw a flow diagram for these expressions:

1)  $4a + 3$  a x 4 + 3

2)  $3 + 2a$  a x 2 + 3

3)  $4a - 3$  a x 4 - 3

4)  $4(3+a)$  a + 3 x 4

5)  $3(a-5)$  a - 5 x 3

Flow diagrams: backwards!

$$4 \xrightarrow{\times 5} 20 \xrightarrow{+ 10} 30$$

$$2 \xrightarrow{\times 3} 6 \xrightarrow{+ 4} 10$$

$$6 \xrightarrow{\times 2} 12 \xrightarrow{- 5} 7$$

$$3 \xrightarrow{\times 10} 30 \xrightarrow{- 5} 25$$

$$6 \xrightarrow{\times 5} 30 \xrightarrow{- 7} 23$$

## Reversing the flow!

$6 \times 5 \rightarrow 30 \rightarrow +10 \rightarrow 40$

$5 \times 3 \rightarrow 15 \rightarrow +4 \rightarrow 19$

$12 \times 2 \rightarrow 24 \rightarrow -5 \rightarrow 19$

$5 \times 10 \rightarrow 50 \rightarrow -5 \rightarrow 45$

$10 \times 5 \rightarrow 50 \rightarrow -7 \rightarrow 43$

$\times 3 \rightarrow +10 \rightarrow 25$

$\times 7 \rightarrow +4 \rightarrow 18$

$\times 2 \rightarrow -15 \rightarrow 7$

$\times 10 \rightarrow -5 \rightarrow 65$

$\times 9 \rightarrow -7 \rightarrow 11$

$\times 5 \rightarrow +10 \rightarrow 30$

$\times 3 \rightarrow +4 \rightarrow 10$

$\times 2 \rightarrow -5 \rightarrow 7$

$\times 10 \rightarrow -5 \rightarrow 25$

$\times 5 \rightarrow -7 \rightarrow 23$

$\times 5 \rightarrow +10 \rightarrow 55$

$\times 3 \rightarrow +1 \rightarrow 22$

$\times 2 \rightarrow -5 \rightarrow 15$

$\times 10 \rightarrow -5 \rightarrow 45$

$\times 5 \rightarrow +5 \rightarrow 40$

## One step Equations

1.  $2x = 10$

$$x = 5$$

2.  $x + 8 = 10$

$$x = 2$$

3.  $5 - x = 2$  (think carefully)

$$x = 3$$

4.  $5x = 45$

$$x = 9$$

6.  $20x = 100$

$$x = 5$$

7.  $x + 11 = 30$

$$x = 19$$

8.  $7x = 84$

$$x = 12$$

9.  $x - 12 = 5$

$$x = 17$$

Check your solutions work!

10.  $15 - x = 10$

$$\underline{\underline{x = 5}}$$

## Solving two step Equations

1.  $2x + 4 = 10$

$x = 3$

$x \rightarrow x \cdot 2 + 4 \rightarrow 10$

$3 \leftarrow 6 \leftarrow 10$

2.  $3x + 1 = 19$

$x = 6$

$x \rightarrow x \cdot 3 \rightarrow +1 \rightarrow 19$

$6 \leftarrow 18 \leftarrow 19$

3.  $5x - 1 = 24$

$x = 5$

$x \rightarrow x \cdot 5 \rightarrow -1 = 24$

$5 \leftarrow 25$

4.  $10x - 4 = 16$

$x = 2$

$x \rightarrow x \cdot 10 \rightarrow -4 \rightarrow 16$

$2 \leftarrow 20$

5.  $12 + 2x = 14$

$x = 1$  ✓

$x \rightarrow x \cdot 2 \rightarrow +12 \rightarrow 14$

$1 \leftarrow 2$

$3x + 1 = 10$

$3x = 10 - 1$

$3x = 9$

$x = 9 \div 3$

$x = 3$

$5x - 4 = 21$

$5x = 21 + 4$

$5x = 25$

$x = 25 \div 5$

$x = 5$

$10x - 3 = 27$

$10x = 27 + 3$

$10x = 30$

$x = 30 \div 10$

$x = 3$

$8x + 6 = 22$

$8x = 22 - 6$

$8x = 16$

$x = 16 \div 8 = 2$

$$3x + 1 = 10$$

$$3x = 10 - 1$$

$$3x = 9$$

$$x = 9 \div 3$$

$$x = 3$$

$$4x - 1 = 15$$

$$4x = 15 + 1$$

$$4x = 16$$

$$x = 16 \div 4$$

$$x = 4$$

$$10x - 1 = 99$$

$$10x = 99 + 1$$

$$10x = 100$$

$$x = 100 \div 10$$

$$x = 10$$

$$5x + 3 = 18$$

$$5x = 18 - 3$$

$$5x = 15$$

$$x = 15 \div 5$$

$$x = 3$$

$$2x + 5 = 27$$

$$2x = 27 - 5$$

$$2x = 22$$

$$x = 22 \div 2$$

$$x = 11$$

$$10 + 3x = 25$$

$$3x = 25 - 10$$

$$3x = 15$$

$$x = 15 \div 3$$

$$x = 5$$

## Solving two - step equations

Have a go at solving these:

1.  $4x + 1 = 9$

$$4x = 9 - 1$$
$$4x = 8$$

2.  $5x + 3 = 8$

$$5x = 8 - 3$$
$$5x = 5$$

$$x = 5 \div 5$$
$$x = 1$$

3.  $6x - 1 = 29$

$$6x = 29 + 1$$

$$6x = 30$$

$$x = 30 \div 6$$

4.  $10x + 3 = 103$

$$10x = 103 - 3 = 100$$

$$10x = 100$$

$$x = 100 \div 10$$

$$x = 10$$

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5.  $4x - 5 = 11$

$$4x = 11 + 5$$

$$4x = 16$$

$$x = 16 \div 4$$

$$x = 4$$

See attachme

Think of a value of  $x$ , make up a 2 stage equation, give it to your partner to solve.

For example:

$$x = 2$$

$$5x = 10$$

$$5x + 10 = 20$$

$$x = 6$$

$$3x = 18$$

$$3x - 2 = 16$$

## Solving problems using equations

**Maria has  $n$  smarties and Emily has 4 more than Maria.**

**Altogether they have 10 smarties.**

**Make and solve an equation to find out how many smarties they each had.**

$$\begin{array}{l} M: n \\ E: n+4 \end{array} \quad \begin{array}{l} 3 \\ 7 \end{array}$$
$$n + n + 4 = 10$$
$$2n + 4 = 10$$
$$\begin{array}{l} 2n + 4 = 10 \\ 2n = 10 - 4 \\ 2n = 6 \\ n = 6 \div 2 \\ \underline{\underline{n = 3}} \end{array}$$

**Ben has  $n$  CDs. Daniel has twice as many as Ben.**

**Altogether they have 99.**

**Make and solve an equation to find out how many CDs they each have.**

$$\begin{array}{l} \text{Ben } n \\ \text{Daniel } 2n \end{array}$$
$$n + 2n = 99$$
$$\begin{array}{l} 3n = 99 \\ n = 99 \div 3 \\ \underline{\underline{n = 33}} \end{array}$$

**There are  $n$  slices of pizza on a plate.**

**Gio eats 3. There are 12 left.**

**Make and solve an equation to find out how many pieces of pizza there were at the start.**



$$\begin{array}{l} n - 3 = 12 \\ n = 12 + 3 \\ \underline{\underline{n = 15}} \end{array}$$

**Back of sheet.**

### Solving equations that have negative x

Work out the solutions to :

1.  $4 - x = 3$   
 $x = 1$

2.  $10 - x = 6$   
 $x = 4$

3.  $15 - x = 7$   
 $x = 8$

A step more difficult is, for example:

4.  $10 - 2x = 6$   
 $2x = 4$   
 $x = 4 \div 2$   
 $x = 2$

5.  $25 - 5x = 10$   
 $5x = 15$   
 $x = 3$

6.  $100 - 11x = 78$   
 $11x = 22$   
 $x = 2$

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(ext qu 2: make sure you write the equation, even if you know the answer).

1)  $30 - x = 20$     2)  $12 - 2x = 6$   
 $x = 10$              $2x = 6$   
                           $x = 3$

3)  $14 - 3x = 5$     4)  $21 - 5x = 11$   
 $3x = 9$              $5x = 10$   
 $x = 3$                $x = 2$

$$\begin{aligned} 5) \quad 12 - 3x &= 0 \\ 3x &= 12 \\ \underline{x} &= \underline{4} \end{aligned}$$

$$\begin{aligned} 6) \quad 25 - 4x &= 5 \\ 4x &= 20 \\ \underline{x} &= \underline{5} \end{aligned}$$

Solving Equations with x on both sides

These are like balances.

$$2x + 10 = 3x + 5 \quad (-2x)$$

$$10 = x + 5$$

$$\underline{\underline{x = 5}}$$

$$6x + 4 = 7x + 1 \quad (-6x)$$

$$4 = x + 1$$

$$\underline{\underline{x = 3}}$$

$$7x - 5 = 6x - 1 \quad (-6x)$$

$$x - 5 = -1$$

$$\underline{\underline{x = 4}}$$

$$12x + 1 = 20x - 15 \quad (-12x)$$

$$1 = 8x - 15$$

$$1 + 15 = 8x \quad \underline{\underline{x = 2}}$$

$$16 = 8x$$

p311 E2-E4

$$1) \quad x + 5 = 2x \quad (-x)$$

$$\underline{\underline{5 = x}}$$

$$2) \quad 3x + 1 = x + 5 \quad (-x)$$

$$2x + 1 = 5$$

$$2x = 4$$

$$\underline{\underline{x = 2}}$$

$$3) \quad 5x - 5 = 3x + 10 \quad (-3x)$$

$$2x - 5 = 10$$

$$2x = 10 + 5$$

$$2x = 15$$

$$\underline{\underline{x = 7.5}}$$

$$4) \quad 10x + 3 = 5x + 13 \quad (-5x)$$

$$5x + 3 = 13$$

$$5x = 10$$

$$5x = 13 - 3 \quad \underline{\underline{x = 2}}$$

Make up an equation for your neighbour to solve:

eg

$$x = 7$$

$$x = 7$$

$$5x = 37$$

$$5x + 2 = 37$$

$$6x + 2 = 20$$

$$6x = 20 - 2$$

$$6x = 18$$

$$x = 18 \div 6$$

$$\underline{\underline{x = 3}}$$

$$5x + 7 = 61$$

$$5x = 61 - 7$$

$$5x = 54$$

$$x = 54 \div 5$$

$$\underline{\underline{x = 10.8}}$$

$$x = 9$$

$$6x = 54$$

$$6x + 7 = 61$$

$$6x = 61 - 7$$

$$6x = 54$$

$$x = 54 \div 6$$

$$x = 9$$

## Solving equations with x on both sides

$$1) 4x + 1 = 3x + 11$$

$$x + 1 = 11$$

$$\underline{\underline{x = 10}}$$

$$(-3x)$$

$$2) 12x - 6 = 9x + 3$$

$$3x - 6 = 3$$

$$3x = 3 + 6$$

$$3x = 9$$

$$\underline{\underline{x = 3}}$$

$$(-9x)$$

$$3) 15x + 3 = 20x - 2$$

$$4) 2x + 1 = x + 5$$

## Multiplying out Brackets

$$2(n+1)=$$

$$3(n+1)=$$

$$5(n-1)=$$

$$10(n+2)=$$

$$12(n-3)=$$

$$2(3n+1)=$$

$$4(5n-2) =$$

## Solving Equations with brackets

$$2(n+1) = 12$$

$$3(n-1) = 12$$

$$5(n+2) = 20$$

$$10(2n - 1) = 30$$

## Attachments

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group solving equations.doc

I'm thinking of a number.doc